

- base quantities: length (m), time (s), mass (kg), temp (K), current (A)
 7 amount of substance (mol), luminous intensity (cd)

- true value - value obtained in an ideal experiment

- uncertainty - limits of measuring equipment + technique

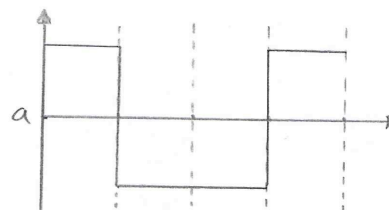
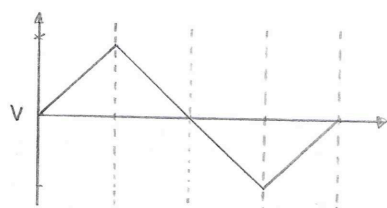
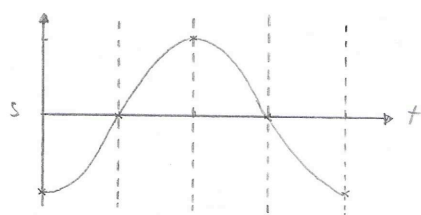
↳ random - different if repeated - average out

↳ systematic - repeating gives same influenced result

- check for zero error

- absolute uncertainty $x \pm \Delta x$

↳ precision of measuring equipment or $\frac{1}{2}$ of range of repeated readings, use the greater



- projectile motion - only force acting is weight

- $v_x = \text{constant}$ $a_x = 0$ $a_y = -g$

- Newton's laws of motion

↳ 1 - an object will remain at rest or in a state of uniform motion unless acted on by a resultant force

↳ 2 - force is the rate of change of momentum $F = \frac{dp}{dt}$

- rate of change of momentum of a body is equal to the resultant force acting on it

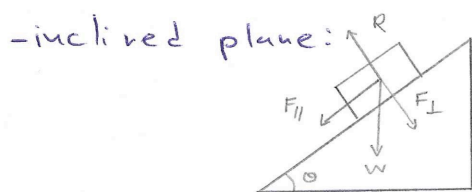
↳ 3 - if object A exerts a force on B, B will exert an equal but opposite force on A.

- mass - amount of matter in a given substance

- the property of a body to resist change in state of motion (measure of inertia)

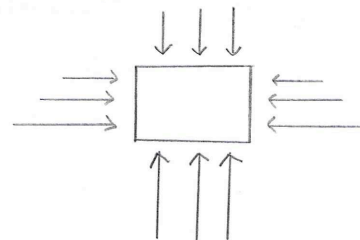
- resistive forces - viscous drag - force an object experiences when moving through a fluid

- upthrust - originates from the pressure difference of fluid on upper and lower surface of object



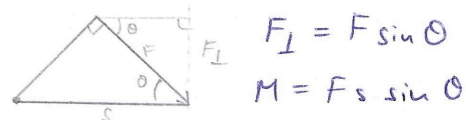
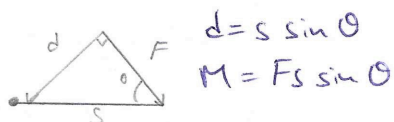
$$F_{\parallel} = W \sin \theta$$

$$F_{\perp} = R = W \cos \theta$$

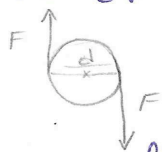


- centre of gravity - point where entire weight appears to act
- centre of mass - point where entire mass seems to be concentrated
- moment - product of force applied and perpendicular distance of the pivot from the line of action of the force

$$M = Fd \quad [M] = \text{Nm}$$



- couple of forces - pair of forces of equal magnitude acting in opposite direction parallel but not along same line



↳ torque of couple = $M_c = Fd$ d - perpendicular distance between lines of action of forces

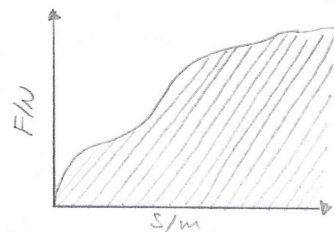
- equilibrium conditions

↳ no net force is acting on it, no net momentum is acting on it

- E - measure of ability of a system to perform work

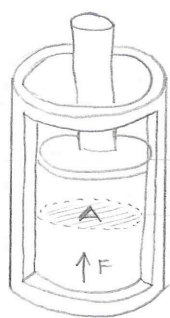
- Work - energy transfer when a force displaces an object $A = W = \int F ds$

$W = Fs$ +ve when done by a force
-ve when done against a force



- law of conservation of E

↳ E can not be created or destroyed only changed in form. total E of system is constant



$$W = Fs \quad P = \text{constant}$$

$$F = PA \quad \Delta V = As$$

$$W = PA s$$

$$= P \Delta V$$

$$W = P \Delta V$$

- GPE - gravitational potential energy
 $\Delta \text{GPE} = mgh$

- KE - kinetic energy
 $\Delta \text{KE} = \frac{1}{2} m (v^2 - u^2)$

- power - rate at which E is transferred
- rate at which work is done

$$P = Fv$$

- motive power - power outputted by a powered object

- efficiency - ratio of useful work to total work $\eta = \frac{W_{\text{useful}}}{W_{\text{total}}}$

- momentum - product of objects mass and velocity

$$p = mv \quad [p] = \text{Ns} = \text{kgms}^{-1} \quad F \Delta t = \Delta p$$

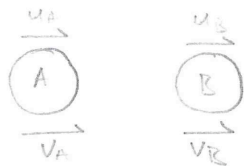
- law of conservation of linear momentum

↳ in an isolated system Σp before and after an event are equal provided no external force acts

- elastic collision - collision in which KE is conserved $e=1$

- inelastic collision - KE not conserved so some dissipated

- perfectly elastic collision - KE conserved



- p conserved

- relative speed of approach = relative speed of separation

$$\vec{v}_B - \vec{v}_A = \vec{u}_A - \vec{u}_B$$

- in explosions initial $p_i = 0$ so also $p_f = 0$

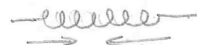
- impulse of a force - J $J = F_{avg} \Delta t = \Delta p$

- density - $\rho = \frac{m}{V}$

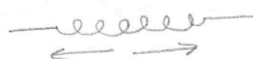
- pressure - normal force acting per unit crosssectional area $P = \frac{F}{A}$

$$P = \rho gh$$

- force applied to spring: - compressive



- tensile



- restoring force - force applied by the spring against force causing the deformation

- hooke's law $F = kx$ $[k] = Nm^{-1}$ $k \approx$ stiffness

- limit of proportionality - point beyond which Hooke's law is no longer obeyed

- elastic limit - point beyond which spring no longer returns to original shape

- plastic deformation

- young modulus - ratio of tensile stress to strain for material

L_0 obeying hooke's law

$$E = \frac{\sigma}{\epsilon} = \frac{FL_0}{Ax}$$



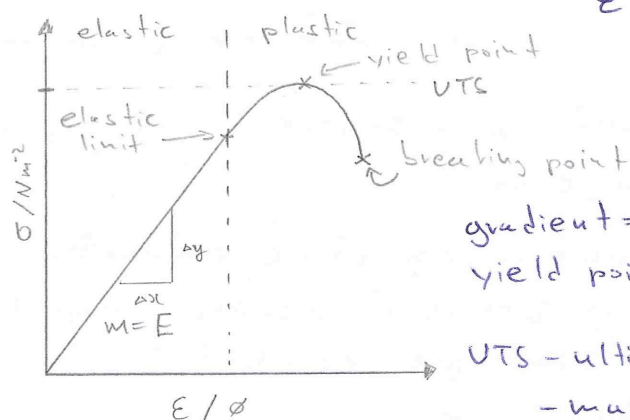
tensile stress

$$\sigma = \frac{F}{A}$$



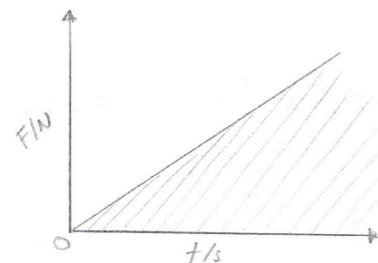
tensile strain

$$\epsilon = \frac{x}{L_0}$$



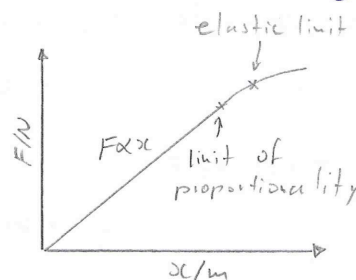
gradient = young modulus
yield point - large increase in extension

UTS - ultimate tensile strength
- max tensile stress



$$A = F_{avg} \Delta t = \frac{1}{2} Lh$$

$$= \int F dt$$

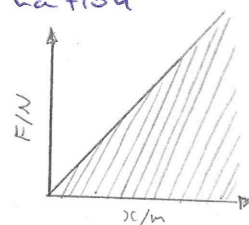


-EPE - elastic potential energy - E stored in a body due to a load (force) causing deformation

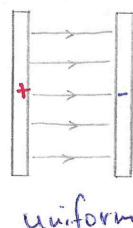
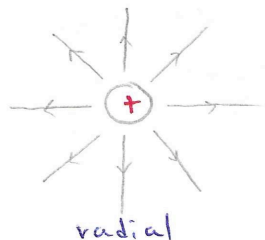
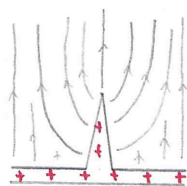
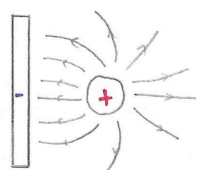
↳ for hookean material

$$EPE = \frac{1}{2} k x^2$$

$$EPE = Fx = A = \int F dx$$



-electric field - region of space where a charged particle experiences a force



radial

uniform

-electric field strength - force experienced at a point per unit charge exerted on a stationary positive charge at a point in the field

$$E = \frac{F}{q}$$

- in a uniform electric field E is constant $E = \frac{V}{d}$ $F = qE$

- current - rate of flow of charge $I = \frac{\Delta Q}{\Delta t}$ $= q \frac{v}{d}$

- e^- drift in random directions overall $\rightarrow +$

- mean drift velocity - steady velocity of e^- colliding with ions as they pass the wire

$-v_d$

- number density - conduction electrons (charge carriers) per unit volume

- n for Cu $n_{Cu} \approx 10^{29} m^{-3}$

$I = nA v_d q$ I - current n - number density A - CS area v_d - mean drift velocity q - charge

- Coulomb - charge which flows past a point in a time of 1s when a current of 1A is flowing

- charge always multiple of e $+e = 1.6 \times 10^{-19} C$

- potential difference - between A, B is the E per unit charge as the unit charge moves from A $\rightarrow$ B

$$V = \frac{W}{Q}$$

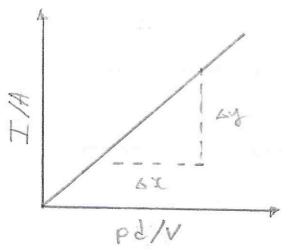
- EMF - E transferred by a source in driving a unit charge around a complete circuit

- Ohm's law - current in an ohmic conductor is proportional to the voltage across it provided temp + other physical conditions are constant

$$V \propto I \quad V = RI \quad \therefore R = \frac{V}{I}$$

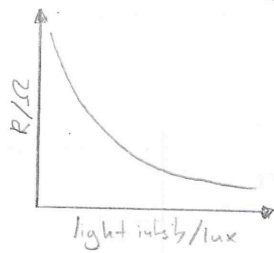
- resistance - measure of the extent to which a material opposes the flow of charge (e^- s) ⑤

- Ohm - resistance of a component when a pd of 1V drives a current of 1A through it



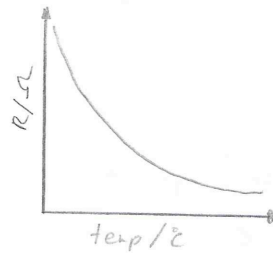
$$m = \frac{1}{R}$$

Ohmic



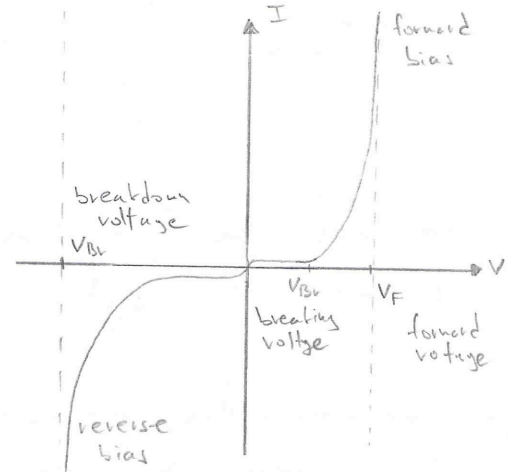
dark $\approx 5M\Omega$
light $\approx 500\Omega$

LDR



NTC $\downarrow$
PTC $\uparrow$

Thermistor



Diode $V_{Br} \approx 0.6V$

LED $V_{Br} \approx 2V$

- as temp $\uparrow$ $R \uparrow$ since $v_d \downarrow$ due to collisions with ions - moving faster so more collisions

- resistors in series $R_T = \sum_{i=1}^n R_i$ resistors in parallel $R_T = \frac{1}{\sum_{i=1}^n \frac{1}{R_i}}$

- Kirchhoff's law

$\hookrightarrow$ 1st law - sum of currents leaving a junction = sum of currents entering the junction

$\hookrightarrow$ 2nd law - sum of emf around any loop in circuit = sum of pds around each loop

- efficiency - measure of how well a device transforms energy to useful forms

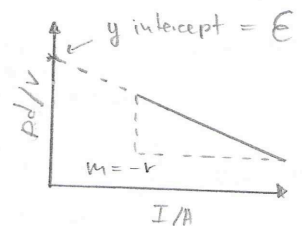
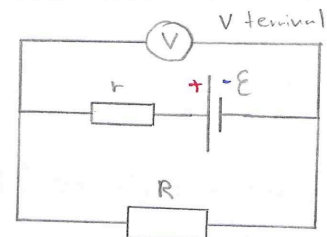
- resistivity - measure of property of material of how much it opposes the flow of charge

$$\rho = \frac{RA}{L} \quad R = \frac{\rho L}{A} \quad P = IV = \frac{V^2}{R} = I^2 R$$

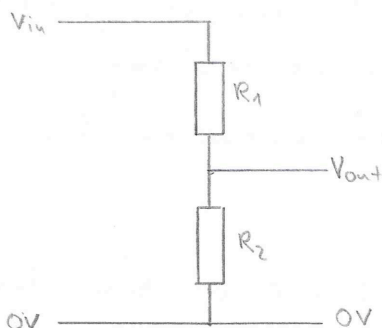
- cell with internal resistance

$$\begin{aligned} \text{terminal pd} &= \text{emf} - \text{lost volts} & \mathcal{E} &= I(R+r) \\ \text{emf} &= \text{terminal pd} + \text{lost volts} & &= V + Ir \end{aligned}$$

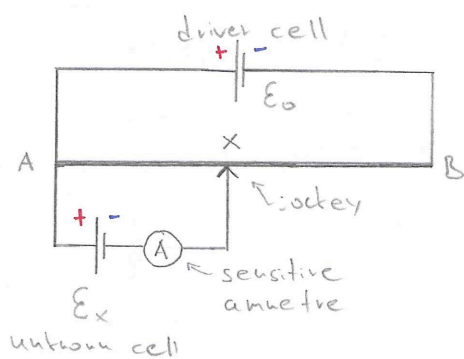
assuming R of $\textcircled{V}$ is ∞ as $R \rightarrow \infty$ $I \rightarrow 0$
 $V_{\text{terminal}} \rightarrow \mathcal{E}$



- potential dividers



$$V_{out} = \frac{V_{in} R_2}{R_1 + R_2} \quad I = \frac{V_{in}}{R_1 + R_2}$$

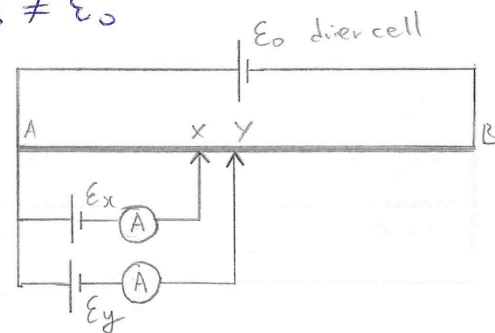


at equilibrium point $I=0$ $V_{AX} = E_x$

r negligible since $I=0$

$$E_x = \frac{AX}{AB} E_0 \quad \text{current still flows in } E_0$$

so $V_{AB} \neq E_0$



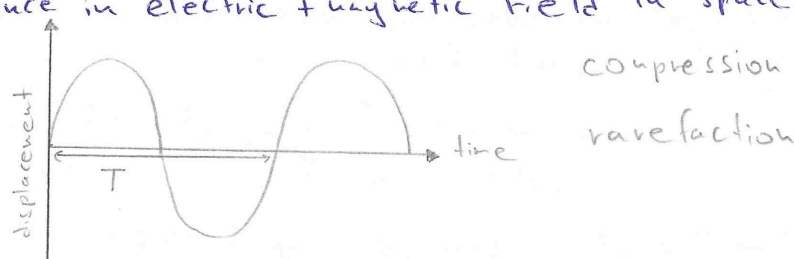
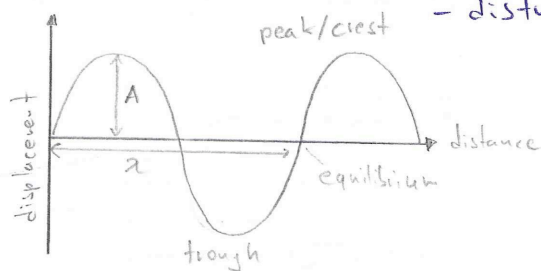
- to overcome this use setup to compare 2 emf's (E_x, E_y)

$$\frac{E_x}{E_y} = \frac{AX}{AY}$$

- wave - periodic disturbance in a medium or space
 - transfer E or info without transferring matter between 2 points
- progressive waves - move outward from the source
 - ↳ 2 types: 1) transverse - oscillates perpendicular to direction of propagation of wave
 - 2) longitudinal - oscillates parallel to direction of propagation of wave
- mechanical waves - oscillations of particles in physical medium
 - do not propagate in vacuum

- electromagnetic waves - produced by acceleration of charge

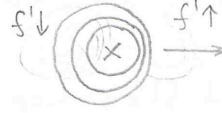
- disturbance in electric + magnetic field in space



- displacement - distance of a particle from equilibrium position
- amplitude - A - maximum displacement
- period - T - time it takes for a particle to make 1 complete oscillation
 - time for object producing wave to complete 1 oscillation
- frequency - f - number of oscillations passing a certain point per unit of time
- wavelength - λ - distance along medium between 2 successive particles with same displacement and phase of motion
- phase difference - ϕ - fraction of a complete cycle between two points on a wave
- wave front - all points which started from the source at same time

- polarised waves - oscillate in a single plane normal to propagation
 - only transverse waves
- when a wave hits a boundary it is reflected with a phase difference
- intensity of a wave - I - power supplied per unit cross-sectional area

$$I = \frac{P}{A} \quad [I] = \text{Wm}^{-2}$$
 - directly proportional to amplitude squared
$$I \propto A^2$$
- $v = f\lambda \quad f = \frac{1}{T}$



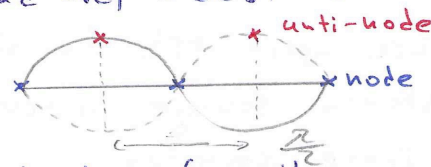
- doppler effect - apparent change in frequency of a wave caused by relative motion between source and observer (redshift in light)
- $$f' = f \frac{(v+v_o)}{(v-v_s)}$$

- all em waves travel at $c = 3.0 \times 10^8 \text{ ms}^{-1}$ in vacuum as they enter a medium $v \downarrow$ f is constant so $\lambda \downarrow$

Radio	Microwave	Infra Red	Visible	Ultra Violet	X rays	γ rays
10^6	10^{-1}	10^{-3}	7×10^{-7}	4×10^{-7}	10^{-8}	10^{-10}
10^{-1}	10^{-3}	7×10^{-7}	4×10^{-7}	10^{-8}	10^{-13}	10^{-16}

- superposition - when 2 or more waves overlap the resultant displacement at a point is equal to the sum of individual displacements at that point
- if both waves in phase (+ve or -ve) = constructive interference
- both waves out of phase (+ve and -ve) = destructive interference

- antinode - maximum displacement
- node - no displacement



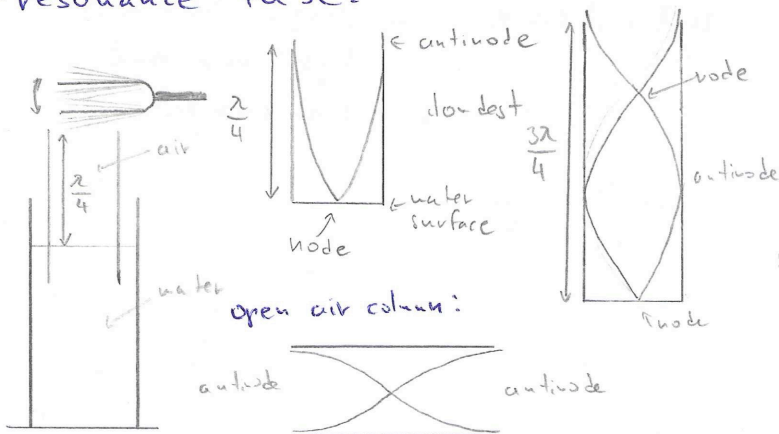
- stationary wave - stores E but doesn't transfer it
- created: - 2 progressive waves of = speed, wavelength, frequency, amplitude travelling in opposite directions superimpose

- λ and f of progressive and stationary wave equal

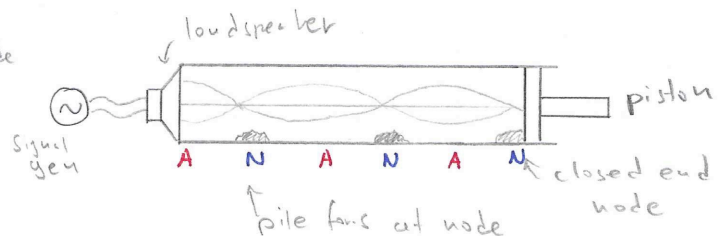
- first fundamental frequency $f_0 = \frac{v}{2L} \quad \lambda = 2L$

- second harmonic $f_1 = \frac{v}{L} \quad \lambda = L$

- resonance tube:



Kundt's experiment
used to determine speed of sound



- diffraction - spreading out/bending of waves as they pass obstacle or through a gap
- ↳ explanation - Huygen - Fresnel principle : each point at wave front acts as infinitesimal wave source to produce secondary waves which superimpose
- monochromatic - emitted with only one f or λ
- coherent - all waves either exactly in phase or at a constant phase difference

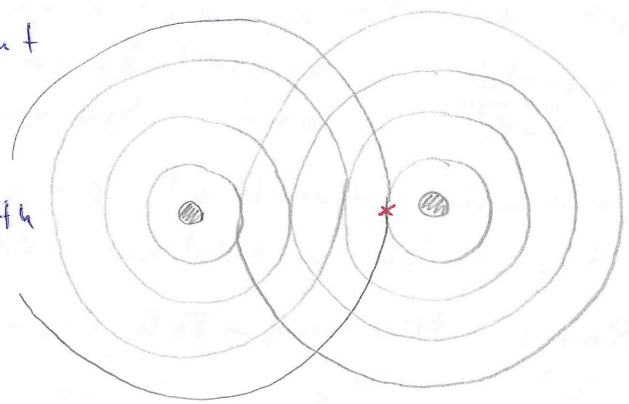
- laser = monochromatic and coherent

- constructive interference

- ↳ path difference between 2 coherent sources = integer multiple of wavelength
- path difference = $n\lambda$ $n \in +\mathbb{Z}$

- destructive interference

- ↳ path difference = $(n + \frac{1}{2})\lambda$ $n \in +\mathbb{Z}$

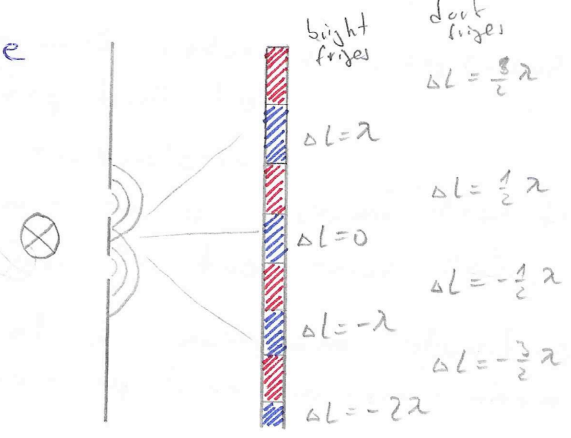


— constructive — destructive

- fringes - places of constructive interference

- conditions for double slit interference

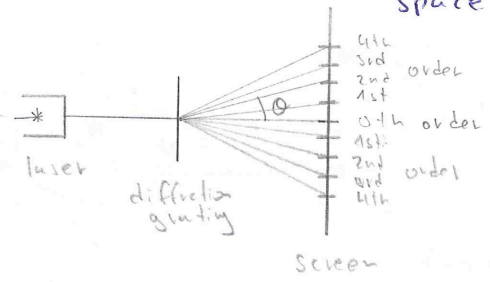
- ↳ coherent waves
- ↳ slit width appropriate for beams to overlap sufficiently
- ↳ suitable distance apart slits for wavelength
- ↳ sufficient distance source $\rightarrow$ screen



$W = \lambda \frac{d}{S}$

W - fringe separation
S - slit separation
d - distance to screen

- diffraction grating - plate with many close spaced parallel slits



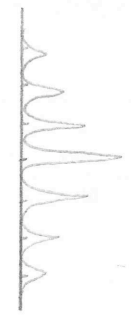
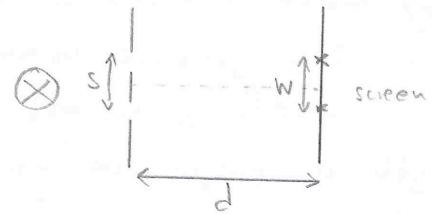
for grating with m lines per metre

$d = \frac{1}{m}$

$n\lambda = \frac{1}{m} \sin \theta$

$n\lambda = d \sin \theta$

n - order of fringe
 θ - angle between light ray and horizontal



- α particle scattering experiment
 - ↳ α particles deviated pass through - repulsive force between α particle and the charged nucleus
 - ↳ most α particles have little or no deviation - atom is mostly empty space
 - ↳ very few deviated at angles $> 90^\circ$ - most mass of atom is concentrated in small space

$$m_e = 9.11 \times 10^{-31} \text{ kg} \quad m_p = 1.67 \times 10^{-27} \text{ kg}$$

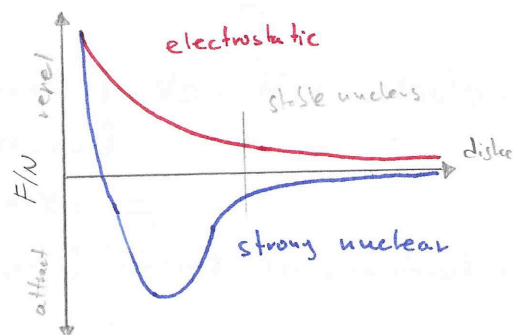
$$r_{\text{proton}} \approx 10^{-15} \text{ m} \quad r_{\text{nucleus}} \approx 10^{-15} - 10^{-14} \text{ m} \quad r_{\text{atom}} \approx 10^{-10} \text{ m}$$

$$A = Z + N$$

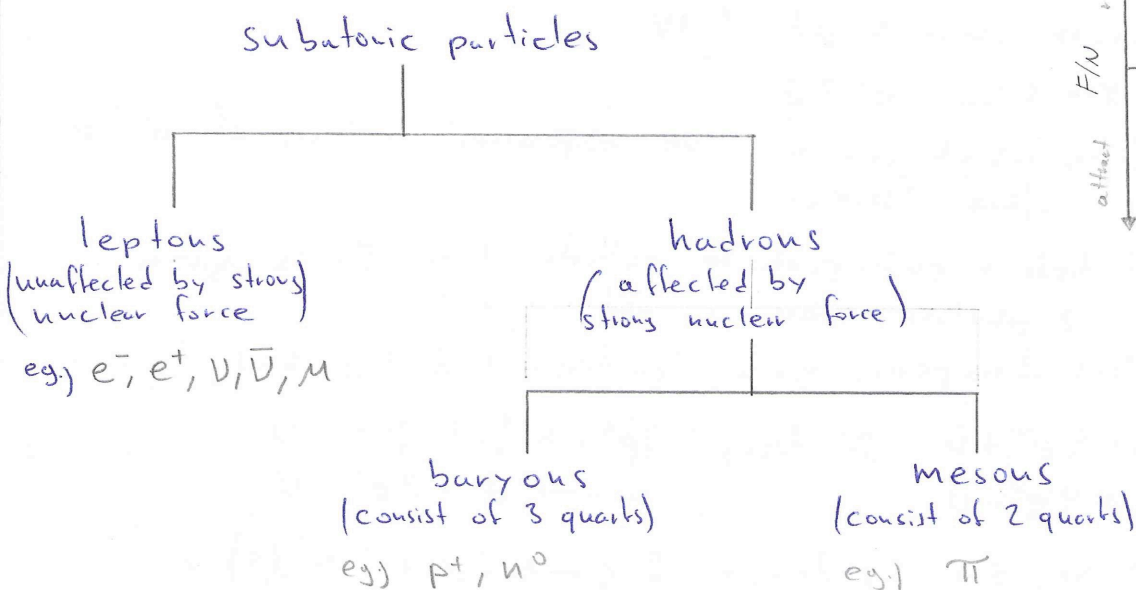
- A - nucleon number Z - proton number N - neutron number
- nucleide - specific combination of protons and neutrons
- isotopes - nuclei of same element $\therefore$ same Z but different number of neutrons N therefore nucleon number A
- ion - electrically non neutral atom (charged)

${}^1_1\text{H}$ protium ${}^2_1\text{H}$ deuterium ${}^3_1\text{H}$ tritium

- Strong nuclear force - acts at small distance $\approx 10^{-14} \text{ m}$
 - cancels out repulsion of p^+ in nucleus
- weak nuclear force - responsible for β decay



baryons are more stable in a nucleus



- p^+ is most stable baryon eventually all baryons decay to p^+

	quarks			anti quarks		
	up u	down d	strange s	up $\bar{u}$	down $\bar{d}$	strange $\bar{s}$
charge	$+\frac{2}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{2}{3}$	$+\frac{1}{3}$	$+\frac{1}{3}$
strangeness	0	0	-1	0	0	+1

Force - Acts on - Range - Exchange particle

Strong Nuclear - quarks - 10^{-15} - gluon

Weak Nuclear - quarks + leptons - 10^{-17} - Z^0, W^+, W^- bosons

Electromagnetic - charged particles - ∞ - photon γ

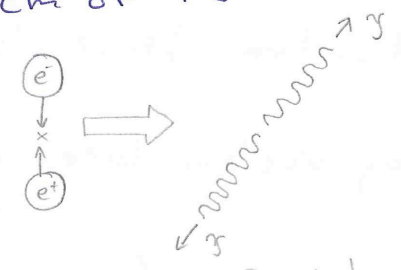
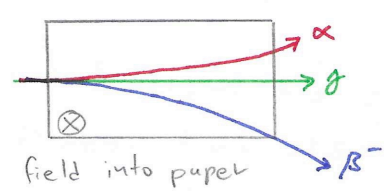
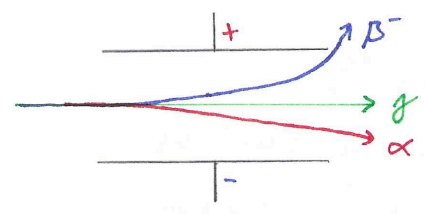
Gravity - particles with mass - graviton

- ionisation - fast moving α/β particle collides or passes near an atom and knock/drag out an e^- forming an ion

- α particle - most ionising - high mass + moves slowly $\therefore$ long interaction
 - low penetrating - 5-6 cm in air stopped by paper
 - cloud chamber, solid state detector, GM tube

- β particle - less ionising - light + moves quickly
 - moderately penetrating - few m of air or mm of Al
 - GM tube for β^- radiation

- γ rays - least ionising - only increases E of e^-
 - most penetrating - m of concrete or cm of Pb



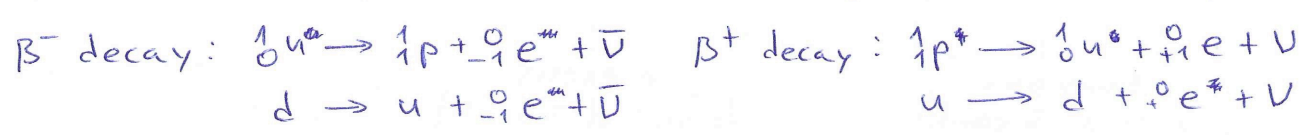
- electron volt - eV - E transferred when an e^- travels through pd of 1V
 - $1\text{eV} = 1.60 \times 10^{-19} \text{ J}$

electron + positron $\rightarrow$ 2 photons

- fundamental force - force which can not be explained in terms of action of other forces

- annihilation - when particle + anti-particle collide their E is given out as 2 photons mass is lost $m \rightarrow E$

- pair production - photons disappear giving particle + antiparticle $E \rightarrow m$



- Neutrinos - little mass, no charge, hard to detect

- β^-/β^+ emitted at range of velocities so something must carry extra E

- charge + mass - energy conserved in decay

- specific charge - charge per unit mass - C/kg

α - $\frac{1}{10}c$ β^-/β^+ - range $\approx \frac{99}{100}c$ γ - c
 4 MeV $\frac{1}{2} \text{ MeV}$ 10 keV - 10 MeV

Feynman diagram:

